

1. Bivariate data

- Two-way frequency tables
  - Explanatory variable eg. Gender
  - Response variable eg. Transport to school

(The explanatory variable is the variable used to explain or predict a difference in the response variable)

	Bus	Car	Train	Other	Totals
Male	26	47	32	19	124
Female	35	70	45	24	174
Male	21%	38%	26%	15%	100%
Female	20%	40%	26%	14%	100%

General Rule:

- If the explanatory variable uses the rows to show its different categories use row percentages (based on row total)
- If the explanatory variable uses the columns to show its different categories use column percentages (based on column total)

2. Bivariate data - further analysis

- Form: linear or non linear
- Direction: Positive or negative
- Strength: Strong, moderate, weak (examples page 42, Unit 3 Maths Apps TextBook)

- Calc: • linear regression [Stats]
- predicted value
  - correlation coefficient (r)
  - coefficient of determination (r<sup>2</sup>)

3. Sequences

Repeatedly:

- adding/taking # +3/-2
- multiplying/dividing # x3/:2

Recursive Rule/Formula

4. Sequences - some specific types

- Arithmetic sequences (AP) (Linear graph)
  - Constant first difference pattern/gradient
  - Diff: +4 = 7, 11, 15, 19, 23...

$$T_{n+1} = T_n + \text{diff}(d), T_1 = \text{1st term}(a)$$

- Geometric sequences (GP) (Exponential graph)
  - Multiplying previous term by constant amount
  - Ratio: 3 = 5, 15, 45, 135, 405...

$$T_{n+1} = \text{ratio}(r) \times T_n, T_1 = \text{1st term}(a)$$

- AP - jumps eg.

$$T_{n+1} = T_n + 7, T_1 = 25$$

$$T_2 = T_1 + 7 = 32$$

$$T_{100} = T_1 + 99(7) = 25 + 693 = 718$$

$$- T_n = a + (n-1)d$$

- GP - jumps

$$T_n = a \times r^{n-1} \text{ or:}$$

Calc: sequences

- Sequences can show growth + decay
- First order linear recurrence relations

$$T_{n+1} = b \times T_n + c$$

$$\text{Eg. } T_{n+1} = 1.2 \times T_n - 50, T_1 = 400$$

$$T_2 = 1.2 \times T_1 - 50 = 430$$

$$T_3 = 1.2 \times T_2 - 50 = 466$$

$$T_4 = 1.2 \times T_3 - 50 = 509.2$$

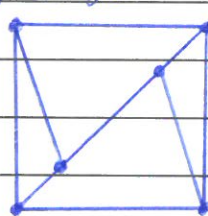
5. Networks

Euler's Rule

$$\text{vertices} + \text{faces} = \text{edges} + 2$$

$$v + f = e + 2$$

eg. Edges?



$$v + f = e + 2$$

$$6 + 5 = e + 2$$

$$11 - 2 = e$$

$$9 = e$$

∴ 9 edges on this network

5. Network cont. Vocab

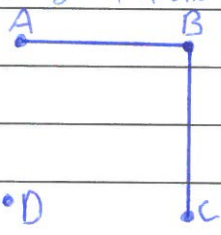
- Loop - any edge that starts and ends at same vertex
- Multiple Edges - if two or more edges connect the same two vertices, then the edges are said to be multiple edges
- Weighted Graph/Network - when each edge is numbered showing a particular value
- Directed Graph/Diagraph - has directed edges (arrows)
- Undirected Graph - no direct edges (no arrows)
- Simple Graph/Network - undirected, unweighted, no loops, no multiple edges
- Simple Directed Graph - simple, arrow
- Simple Weighted Graph - simple, weighted

WALKS:

- Closed - starts + finishes at same vertex
- Open - doesn't finish at starting vertex
- Path - a walk, no repeated use edge or vertex
- Open Path - starting + finish vertices different
- Closed Path - finishes at starting vertex
- Trail - no repeated use of an edge
- Closed Trail - ends at vertex it started from
- Length of Walk, Path, Trail - # of edges travelled

VERTICES

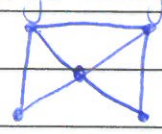
- Connected: B+C
- Adjacent: A+B
- Unconnected: A+D



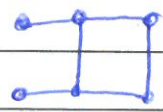
- Complete Graph - every vertex is connected to every one by single edge
- Bridge - in connected network, any edge which, when removed, leaves the network disconnected
- Connections with directed networks - with directed networks we instead

• Traversability - can it be drawn without taking the pen off the paper and without going over the same edge twice (can go through vertices)?

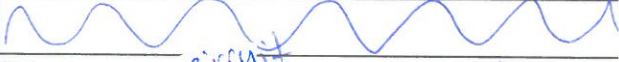
Traversable:



Not Traversable:

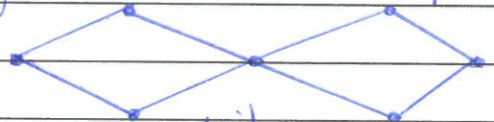


• Planar graphs - can be drawn with its edges only intersecting at vertices



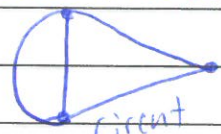
Eulerian <sup>circuit</sup> - a connected graph, travels every edge once and only once, repeated vertices permitted

eg.



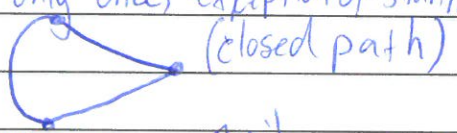
Semi-Eulerian <sup>trail</sup> - a connected graph, open trail, every edge only once, must have two odd vertices

eg.



Hamiltonian <sup>circuit</sup> - every vertex in a graph only once, exception of start/finish

eg.



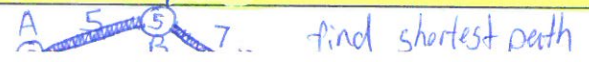
Semi Hamiltonian <sup>trail</sup> - open path that includes every vertex in graph once



Eulerian - no odd vertices

Semi-Eulerian - 2 odd vertices

6. Shortest path



find shortest path